Tableau 5. Distances interatomiques ( $\AA$ ) et angles $\left({ }^{\circ}\right)$ caractérisant les liaisons hydrogène

Code de symétrie


Distances intermoléculaires I $\cdots$ I inférieures à $4,300 \AA$

| $\mathrm{I}(1) \cdots \mathrm{l}\left(1^{\text {iiI }}\right)$ | $4,276(2)$ | $\mathrm{I}(1) \cdots \mathrm{I}\left(2^{v}\right)$ | $4,178(2)$ |
| :--- | :--- | :--- | :--- |
| $\mathrm{l}(1) \cdots \mathrm{I}\left(2^{\text {ii }}\right)$ | $4,265(2)$ | $\mathrm{I}(2) \cdots \mathrm{l}\left(2^{\text {vi }}\right)$ | $3,961(2)$ |

## Liaisons hydrogène

La cohésion de l'édifice cristallin est assurée par des interactions de type ionique et des liaisons de faible énergie. Le Tableau 5 indique les distances interatomiques et les angles caractérisant l'existence de liaisons hydrogène intermoléculaires ainsi que les contacts de van der Waals I $\cdots$ I inférieurs à $4,30 \AA$.

Chaque atome d'iode est accepteur d'un proton du groupement amine protoné $\mathrm{NH}_{3}^{+}$, les distances les plus courtes se trouvant entre $\mathrm{N}-\mathrm{H}^{\prime}(\mathrm{N}) \cdots \mathrm{I}(1)(3,624 \AA$ ) et $\mathrm{N}-\mathrm{H}^{\prime \prime}(\mathrm{N}) \cdots \mathrm{I}(3)(3,688 \AA)$. L'atome d'hydrogène du groupement OH participe à des liaisons hydrogène entre molécules organiques.

Dans ce complexe le cation organique n'a aucune influence sur la régularité des octaèdres $\mathrm{Tel}_{6}^{2-}$ et comme dans les composés analogues la stabilité de l'édifice cristallin est assurée par un réseau de liaisons hydrogène et des contacts de van der Waals.

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# The Crystal and Molecular Structure of the Tetrafluoroborate, Hexafluoroantimonate and Hexafluorophosphate Salts of the Bicyclo[5.4.1]dodecapentaenylium Ion 

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#### Abstract

The molecular and crystal structures of three salts of the bicyclo[5.4.1]dodecapentaenylium cation, $\mathrm{C}_{12} \mathrm{H}_{11}^{+}$, namely the tetrafluoroborate, $\mathrm{BF}_{4}^{-}$, the hexafluoro-


antimonate, $\mathrm{SbF}_{6}^{-}$, and the hexafluorophosphate, $\mathrm{PF}_{6}^{-}$, have been solved by X-ray diffraction. All the crystals were affected by disorder and consequently a number of problems made solution and refinement particularly difficult. However, the body of our results points © 1979 International Union of Crystallography
unequivocally to the classification of the cation as a perturbed [11]annulenium system.

## Introduction

The synthesis of stable salts (tetrafluoroborate and perchlorate) of the bicyclo[5.4.1]dodecapentaenylium cation (hereinafter BDP) was first reported by Grimme, Hoffmann \& Vogel (1965). The structure of this ten $\pi$ electron system has been investigated on the basis of its electronic spectra by Grimme, Heilbronner, Hohlneicher, Vogel \& Weber (1968), and by interpretation of the ${ }^{13} \mathrm{C}$ NMR chemical shifts by Kemp-Jones, Jones, Sakai, Beeman \& Masamune (1973). The former authors have regarded the ion as a perturbed [11]annulenium system (I), whereas the latter have suggested a benzohomotropenylium structure (II), where a significant electron overlap between $\mathrm{C}(1)$ and $\mathrm{C}(6)$ ( $c f$. Fig. 2) is present. Using a perturbational molecular orbital approach, Haddon (1975) has considered the effect of a 1-6 transannular interaction on the annulene system, and evaluated the implied energy change. This treatment, however, cannot predict to what extent the molecule avails itself of the resulting extra stabilization. In the light of our preliminary account of the X-ray analysis of BDP hexafluorophosphate (Destro, Pilati \& Simonetta, 1976), Haddon (1977) later reinvestigated the ion, focusing in particular on the experimental bond lengths. His study has suggested that the electronic structure of BDP is determined by a complex interplay of perturbations. We report here the complete and up-to-date results of the X-ray determination of the BDP geometry, a part of the systematic investigation of the conformation of bridged annulenes, which have long been a subject of interest in our laboratory (see, for example, Destro \& Simonetta, 1977; Simonetta, 1974). Our work was initiated in 1969 with the analysis of BDP tetrafluoroborate. Some years later a second derivative, the hexafluoroantimonate salt, was available and analyzed. Recently, low-temperature and highresolution data of a third salt, BDP hexafluorophosphate, were collected and a satisfactory description of the structure could be obtained. All the samples studied were kindly supplied by Professor E. Vogel, whom we deeply thank.

(I)

(II)

## The $\mathrm{BF}_{4}^{-}$salt

Most of the crystals, in the form of yellow-orange needles, were twinned and showed apparent ortho-
rhombic symmetry on preliminary Weissenberg photographs. Correct monoclinic symmetry was indicated by a thin crystal 0.2 mm long (cross section $0.1 \times 0.05$ mm ), which was used to obtain cell parameters (Table 1) by film measurements, essentially following the Straumanis technique. Even after prolonged exposure, only a few intensities were detectable at $\sin \theta / \lambda>0.42$ $\AA^{-1}$. This fact, together with the appearance of diffuse streaks in the vicinity of strong reflexions, was indicative of possible structural disorder. The systematic absences, $h 0 l$ for $l$ odd, $0 k 0$ for $k$ odd, and $h k l$ for $h+k$ odd, are common to three space groups, $C 2$, $C m$ and $C 2 / m$. (The conventional $C$-centered unit cell was preferred to the $I$-centered cell with $a=10.941$, $b=9.965, c=11.085 \AA, \beta=104.97^{\circ}$.)

Intensity data were collected from multiple-film equiinclination Weissenberg photographs (layers 0-8 around $b$ and $0-2$ around $a$ ) with Ni-filtered $\mathrm{Cu} K a$ radiation $(\lambda=1.5418 \AA$ ). After processing of the data (Lorentz and polarization factors applied, no correction for absorption), only 552 reflexions out of 1135 explored had net intensities above background.

Several attempts to solve the structure based on the interpretation of the Patterson synthesis (program written by Filippini \& Gramaccioli, 1969) or on direct methods, using first the computer program of Long (1965) and then the early version of programs written in our laboratory (Bianchi, Destro \& Gavezzotti, 1972), were unsuccessful.

A possible reason for the failure of direct methods was the paucity of measurable intensities, especially at high $\sin \theta / \lambda$ values. Therefore, our efforts were devoted to the attainment of larger crystals, with the aim of increasing the number of reliable observations. Several crystallization procedures were tried with different mixtures of solvents (glacial acetic acid, ethanol and acetonitrile) at different temperatures. The best result consisted of a single crystal of dimensions $0.30 \times 0.18$ $\times 0.08 \mathrm{~mm}$, which was used to collect a second set of data on a General Electric diffractometer automated by Datex, with Ni-filtered copper radiation and a propor-

Table 1. Crystal data

| Anion | $\mathrm{BF}_{4}^{-}$ | $\mathrm{SbF}_{6}^{-}$ | $\mathrm{PF}_{6}^{-}$ |  |
| :--- | :--- | :--- | :--- | :--- |
| $T(\mathrm{~K})$ | 295 | 290 | 290 | 110 |
| $a(\AA)$ | $13.413(5)$ | $16.077(3)$ | $15.794(4)$ | $15.478(4)$ |
| $b$ | $9.965(3)$ | $7.083(2)$ | $6.904(1)$ | $6.821(2)$ |
| $c$ | $11.085(5)$ | $11.622(2)$ | $11.444(3)$ | $11.373(3)$ |
| $\beta\left({ }^{\circ}\right)$ | $128.00(6)$ | 90 | 90 | 90 |
| $V\left(\AA^{3}\right)$ | 1167.6 | 1323.4 | 1247.9 | 1200.7 |
| Space group | $C 2 / m$ | $P c a m$ | $P c a m$ | Pcam |
| $D_{m}\left(\mathrm{Mg} \mathrm{m}^{-3}\right)$ | 1.37 | 1.96 | 1.59 | - |
| $D_{x}$ | 1.376 | 1.962 | 1.598 | 1.660 |
| $\mu\left(\mathrm{Cu} \mathrm{Ka}^{2}\right)$ | 1.10 | 17.75 | 2.57 | 2.67 |
| $\left(\mathrm{~mm}^{-1}\right)$ |  |  |  |  |
| $\mu\left(\mathrm{Mo} \mathrm{Ka}^{2}\right)$ | 0.13 | 2.17 | 0.29 | 0.30 |
| $M_{r}$ | 242.0 | 391.0 | 300.2 | 300.2 |
| $Z$ | 4 | 4 | 4 | 4 |

tional counter. A $\theta-2 \theta$ scan technique was used, the scan range including both the $\alpha_{1}$ and $\alpha_{2}$ peaks; background was counted for 20 s at each end of the scan, and the scanning rate was $0.5^{\circ}$ in $2 \theta$ per min.

A single standard reflexion was checked after each 15 intensity measurements; it showed no significant drift in intensity. All the measured intensities, 1309 in number, were corrected for background and then for Lorentz and polarization factors; no correction for absorption was deemed necessary. Observational variances $\sigma^{2}(I)$ included, in addition to counting statistics for the scan and backgrounds, a term ( 0.02 $\times S)^{2}$, where $S$ is the scan count.

(b)

Fig. 1. Electron-density projections on (010) in $(a)$ the cation and (b) the $\mathrm{BF}_{4}^{-}$anion regions; contours are at arbitrary intervals. The superposition of the models adopted in describing the disorder is shown.
$163 E$ 's $>1.5$ were derived from the 702 reflexions with net intensities above background. The phase determination was again tried by symbolic addition. At the end of this process, which was carried out by hand, 76 phases were confidently assigned and subsequently used for the usual tangent-formula expansion. (It is worth noting that this starting set included 11 E 's, with $k>8$, not measured on the Weissenberg photographs; moreover, eight reflexions, here with $E>1 \cdot 9$, had been assigned $E$ values $<1.0$ in the previous treatment.) A Fourier map based on the 163 phased $E$ 's was then computed. Its main features were similar to those of the final electron-density map (Figs. 1 and 2 ) in the region of the cation, while only two peaks at $y=0$ were possibly related to the anion atoms. All attempts to interpret the map with ordered structures, both in centrosymmetric and non-centrosymmetric


Fig. 2. BDP electron density in the $\mathrm{BF}_{4}^{-}$salt. The map is viewed in the direction perpendicular to the ring plane. Besides the crystallographic mirror plane at $y=0$, a pseudo-mirror relates (statistically) one cation (full line) to the other (dotted line).

Table 2. Fractional coordinates $\left(\times 10^{4}\right)$ for the $\mathrm{BF}_{4}^{-}$salt structure
No e.s.d.'s are given, since the ions were refined as rigid groups (see text). Non-primed and primed atoms define the four distinct groups used to interpret the disordered structure.

|  | $x$ | $y$ |  | $x$ | $y$ | $y$ |  |
| :--- | ---: | ---: | ---: | :--- | ---: | ---: | ---: |
| B | 3390 | 0 | 1983 | $\mathrm{~B}^{\prime}$ | 3321 | 0 | 1870 |
| $\mathrm{~F}(1)$ | 2312 | 0 | 1832 | $\mathrm{~F}\left(1^{\prime}\right)$ | 3414 | 0 | 3153 |
| $\mathrm{~F}(2)$ | 4395 | 0 | 3483 | $\mathrm{~F}\left(2^{\prime}\right)$ | 4491 | 0 | 2253 |
| $\mathrm{~F}(3)$ | 3427 | 1106 | 1308 | $\mathrm{~F}\left(3^{\prime}\right)$ | 2689 | 1106 | 1036 |
| $\mathrm{C}(1)$ | 1959 | -1152 | 5552 | $\mathrm{C}\left(1^{\prime}\right)$ | 1589 | 1152 | 4869 |
| $\mathrm{C}(2)$ | 2502 | -1595 | 7046 | $\mathrm{C}\left(2^{\prime}\right)$ | 561 | 1595 | 3400 |
| $\mathrm{C}(3)$ | 3207 | -698 | 8260 | $\mathrm{C}\left(3^{\prime}\right)$ | -26 | 698 | 2180 |
| $\mathrm{C}(9)$ | -191 | 0 | 2180 | $\mathrm{C}\left(9^{\prime}\right)$ | 3037 | 0 | 8278 |
| $\mathrm{C}(10)$ | 103 | -1268 | 2814 | $\mathrm{C}\left(10^{\prime}\right)$ | 2661 | 1268 | 7648 |
| $\mathrm{C}(11)$ | 906 | -1814 | 4324 | $\mathrm{C}\left(11^{\prime}\right)$ | 1861 | 1814 | 6138 |
| $\mathrm{C}(12)$ | 2514 | 0 | 5312 | $\mathrm{C}\left(12^{\prime}\right)$ | 2362 | 0 | 5039 |
| $\mathrm{H}(2)$ | 2377 | -2484 | 7287 | $\mathrm{H}\left(2^{\prime}\right)$ | 195 | 2484 | 3186 |
| $\mathrm{H}(3)$ | 3691 | -1132 | 9277 | $\mathrm{H}\left(3^{\prime}\right)$ | -618 | 1132 | 1169 |
| $\mathrm{H}(9)$ | -856 | 0 | 1100 | $\mathrm{H}\left(9^{\prime}\right)$ | 3524 | 0 | 9367 |
| $\mathrm{H}(10)$ | -375 | -1945 | 2218 | $\mathrm{H}\left(10^{\prime}\right)$ | 2824 | 1945 | 8261 |
| $\mathrm{H}(11)$ | 809 | -2665 | 4682 | $\mathrm{H}\left(11^{\prime}\right)$ | 1399 | 2665 | 5809 |
| $\mathrm{H}(12 A)$ | 3390 | 0 | 6067 | $\mathrm{H}\left(12 A^{\prime}\right)$ | 2411 | 0 | 4235 |
| $\mathrm{H}(12 B)$ | 2339 | 0 | 4334 | $\mathrm{H}\left(12 B^{\prime}\right)$ | 3207 | 0 | 5982 |

space groups, were unsuccessful, and disorder had to be introduced. The fitting of the electron density necessitated, for the cation, the superposition of two annulene systems, as depicted in Figs. 1 and 2, and corresponds physically to a random reversal of direction of successive BDP ions in the crystal. Two $\mathrm{BF}_{4}^{-}$groups with their boron atoms almost coincident, and rotated with respect to each other by $60^{\circ}$ around an axis parallel to $\mathbf{b}$, completed the interpretation of the disordered structure.

The positional and thermal parameters of the model were settled by successive difference Fourier syntheses; this procedure led to $R=0.28$ for the 437 reflexions with $I>2 \sigma(I)$.

High interactions between the parameters of pairs of atoms less than $1.0 \AA$ apart (statistically) prevented any further refinement by usual least-squares techniques. In any case, the correctness of the interpretation of the structure was confirmed when a more reliable geometry for the cation became available, i.e. after the solution of the structure of the hexafluorophosphate salt (see below). From the isotropic refinement of the cation atoms of that structure, a rigid model with exact $m$ symmetry was derived for BDP, and placed in the cell of the $\mathrm{BF}_{4}^{-}$salt in such a way as to roughly coincide with one of the two models illustrated in Fig. 2. From this model, the second one was obtained by a $180^{\circ}$ rotation around the inertial axis perpendicular to the ring plane, and constrained refinement was performed with the program written by Bianchi, Pilati \& Simonetta (1978). The following parameters were varied simultaneously: the scale factor, the $2+2$ coordinates of the center of mass of the two cations, the two angles of rotation (one for each cation) of the rigid groups around the inertial axis

Table 3. Rigid-body-motion parameters for the $\mathrm{BF}_{4}^{-}$ salt

The tensors are referred to a Cartesian coordinate system coincident with the principal inertial axes $L, M$ and $N$. For the anion, $N$ was assumed parallel to the crystallographic $b$ axis. All components of the tensors have been multiplied by $10^{4}$.

|  | $\mathrm{BF}_{4}^{-}$ | BDP |
| :--- | ---: | ---: |
| $T_{11}\left(\AA^{2}\right)$ | $1017(74)$ | $351(48)$ |
| $T_{22}$ | $654(60)$ | $956(53)$ |
| $T_{33}$ | $906(55)$ | $1140(70)$ |
| $T_{12}$ | $-143(58)$ | 0 |
| $T_{13}$ | 0 | $-21(35)$ |
| $L_{11}\left(\mathrm{rad}^{2}\right)$ | $707(56)$ | $135(31)$ |
| $L_{22}$ | $947(83)$ | $124(15)$ |
| $L_{33}$ | $492(56)$ | $41(23)$ |
| $L_{12}$ | $-252(59)$ | 0 |
| $L_{13}$ | 0 | $24(21)$ |
| Eigenvalues of $\mathbf{L}\left(\mathrm{rad}^{2}\right)$ | 0.109 | 0.014 |
|  | 0.057 | 0.013 |
|  | 0.048 | 0.003 |

parallel to $\mathbf{b}$, the non-zero components of $\mathbf{T}$ and $\mathbf{L}$ tensors (assumed equal for both cations),* and the corresponding parameters for the two $\mathrm{BF}_{4}^{-}$rigid tetrahedra ( $\mathrm{B}-\mathrm{F}=1.35 \AA$ ). The population factor was kept fixed at 0.5 for both ions.

Convergence was assumed when no parameter shift was greater than $5 \%$ of its standard deviation. The corresponding $R$ was 0.13 and the $R_{w}$ index 0.14 for the 437 reflexions [with $I>2 \sigma(I)$ ] on which the refinement of the 29 parameters was based ( $R=0.17$ including all reflexions with $I>0$ ). A difference map revealed residues up to $0.43 \mathrm{e} \AA^{-3}$ in the vicinity of the $\mathrm{BF}_{4}^{-}$groupings. This could suggest a possible third orientation of the anion or, more likely, simply reflect the inadequacy of describing the thermal anisotropy by an ellipsoidal motion. Further pursuit of model fitting did not seem economical. The final coordinates are given in Table 2, while Table 3 reports the rigid-bodymotion parameters. $\dagger$

The $\mathrm{C}(1) \cdots \mathrm{C}(6)$ transannular distance, $2 \cdot 30 \AA$, is worth mentioning, since it indicates that the correct way of describing the BDP system is as an annulenium ion, rather than a benzohomotropylium cation.

The packing arrangement of the ions in the structure is shown in Fig. 3. The disorder does not lead to any unusual approach distances between ions; the closest F…C contact is $3.16 \AA$, and there are no C...C distances below $3 \cdot 4 \AA$.

[^0]

Fig. 3. Packing arrangement in the tetrafluoroborate salt. For the sake of clarity, only one model for the BDP cation has been reported.

## The $\mathbf{S b F}_{6}^{-}$salt

Crystals of BDP hexafluoroantimonate are wellformed, square-based bipyramids. A small sample, $0.15 \times 0.15 \times 0.12 \mathrm{~mm}$, was used to derive cell dimensions (Table 1) and counter data. Accurate unitcell parameters were obtained by the fitting of $\sin ^{2} \theta$ values of 60 counter reflexions. Systematic absences $h 0 l, h \neq 2 n$ and $0 k l, l \neq 2 n$ indicate the space groups Pcam or Pca ${ }_{1}$.

Intensity data were collected on a Syntex $P \overline{1}$ diffractometer, using Nb -filtered Mo $K_{\mathrm{a}}$ radiation. Essentially the same procedure described for the counter-data collection of the $\mathrm{BF}_{4}^{-}$salt (see above) was followed. Owing to the small dimensions of the crystal, no absorption correction was applied during the processing of the data, the linear absorption coefficient of $\mu=$ $2.17 \mathrm{~mm}^{-1}$ for Mo $K \kappa$ radiation suggesting that absorption factors range between 1.15 and 1.35 . After the usual corrections for background, Lorentz and polarization factors were applied, the final set $(2 \theta<$ $55^{\circ}$ ) consisted of 1600 reflexions, of which only 183 had negative net intensities. The overall $B$ temperature factor derived by a Wilson (1949) plot had a value of $4.5 \AA^{2}$, which falls in the usual range. Intensity statistics did not allow a safe choice of the space group; tests based on the Wilson (1949) statistics indicated a distribution midway between centric and non-centric, with perhaps a slight predominance of the latter. A three-dimensional sharpened Patterson function was computed, from which a preliminary structure consistent with space group Pcam could be readily assigned to the anion group. The structure was checked by computation of an electron density map calculated from phases based on the antimony atom alone. Since there are four molecules of $\mathrm{C}_{12} \mathrm{H}_{11} \mathrm{SbF}_{6}$ in the unit cell, and there are eight equivalent positions in the centrosymmetric space group Pcam, the molecule should lie on the mirror plane. Hence, the BDP cation was expected to appear in the map with atoms $C(9)$ and $\mathrm{C}(12)$ on the mirror plane. In contrast, as illustrated


Fig. 4. Projection down the $b$ axis of the electron density of BDP in the hexafluoroantimonate salt; contours are at arbitrary intervals. Two plausible models for the interpretation of the disorder are shown; they are related by the crystallographic mirror plane at $z=0.25$.
in Fig. 4, the electron density corresponded to a BDP ion with its longest direction parallel to c, with the bridge atoms $C(1), C(6)$ and $C(12)$ lying almost exactly on the mirror plane. None of the possible ordered structures in the space group Pca2, was found to be correct, although least-squares refinement with anisotropic atoms for the $\mathrm{SbF}_{6}^{-}$group and isotropic C atoms led to $R$ values as low as 0.05 . Rather unrealistic bond distances ( 1.30 to $1.56 \AA$ ) along the annulene perimeter, exceedingly high values of the $B$ 's of the C atoms (up to $12 \AA^{2}$ ), and large residues (up to $0.79 \mathrm{e} \AA^{-3}$ ) systematically occurring between pairs of atoms of the ring were indicative of a disordered structure in the space group Pcam. However, since the contribution to structure factor amplitudes of 'half' carbon atoms relative to that of the Sb atoms would be similar to that of H atoms in ordinary light-atom structures, any extensive search for plausible models of BDP did not seem worthwhile.*

Thermal-motion analysis of the $\mathrm{SbF}_{6}^{-}$group did not give any evidence of disordering for the fluorine atoms; the $\mathrm{Sb}-\mathrm{F}$ distances are in the range 1.79 (2)-1.87 (2) $\AA$, and the bond angles vary between 87 (1) and $94(1)^{\circ}$. The transannular $\mathrm{C}(1) \cdots \mathrm{C}(6)$ distance in BDP, in the range $2 \cdot 3-2 \cdot 5 \AA$ depending on the various models tested, is in agreement with an annulenium structure, and confirms the value found in the $\mathrm{BF}_{4}^{-}$salt.

## The $\mathbf{P F}_{6}^{-}$salt

The close similarity of the cell dimensions of this compound with those of the hexafluoroantimonate salt (Table 1) and the identity of the systematic absences in


Fig. 5. BDP electron density from low-temperature data of the hexafluorophosphate salt. Comparison with Fig. 2 shows the improvement in resolution.
both cases were indicative of isomorphism. Indeed, structure factor calculations and density maps computed with coordinates derived from the previously studied salt (with the obvious adjustment of the fluorine coordinates to take into account the shortening of $\mathrm{P}-\mathrm{F}$ bond lengths with respect to $\mathrm{Sb}-\mathrm{F}$ distances) reproduced the same situation found there. Contradistinctively, however, the refinement of the ordered BDP model in space group Pca2 ${ }_{1}$, which gave low $R$ values but poor geometry in the case of the $\mathrm{SbF}_{6}^{-}$salt, here did not even converge. The calculations were based on room-temperature data, accurately measured on a Syntex $P \overline{1}$ diffractometer using graphite-monochromated Mo Ka radiation. The set consisted of 1332 reflexions, of which 180 had net intensities below background. The most reliable fit to these data was obtained by an ordered $\mathrm{PF}_{6}$ group with phosphorus and two fluorine atoms lying on a mirror plane (space group Pcam), and a disordered cation obtained by superposition of two annulene systems with their seven- and eight-membered rings interchanged; bridge atoms $\mathrm{C}(1)$, $C(6)$ and $C(12)$ are displaced from the mirror plane, all in the same direction, by $<0 \cdot 3 \AA$.

To refine adequately this model structure, new data were collected at 110 K , measuring all reflexions ( 1449 in number) included in the copper sphere ( $2 \theta_{\mathrm{Mo}}=55^{\circ}$ ), all those having $I>3 \sigma(I)$ in the range $55<2 \theta<106^{\circ}$

Table 4. Fractional coordinates ( $\times 10^{4}$ ) with standard deviations for the $\mathrm{PF}_{6}^{-}$salt structure

|  | $x$ | $y$ | $z$ |
| :---: | :---: | :---: | :---: |
| P | 1139 (1) | 887 (1) | 2500 (0) |
| F(1) | 423 (1) | 592 (1) | 1510 (1) |
| F(2) | 1855 (1) | 1183 (1) | 1510 (1) |
| F(3) | 953 (1) | 3200 (1) | 2500 (0) |
| F(4) | 1325 (1) | -1426 (1) | 2500 (0) |
| C(1) | 1221 (1) | 3970 (3) | 7695 (3) |
| C(2) | 903 (2) | 3526 (6) | 8822 (4) |
| C(3) | 1091 (4) | 4606 (9) | 9803 (5) |
| C(4) | 1395 (4) | 6507 (9) | 9862 (5) |
| C(5) | 1579 (2) | 7754 (6) | 8959 (4) |
| C(6) | 1725 (1) | 7126 (3) | 7793 (3) |
| C(7) | 1582 (2) | 8526 (5) | 6844 (4) |
| C(8) | 1500 (3) | 7704 (9) | 5661 (4) |
| C(9) | 1289 (4) | 5921 (6) | 5175 (6) |
| $\mathrm{C}(10)$ | 936 (3) | 4181 (9) | 5551 (4) |
| C(11) | 795 (2) | 3407 (5) | 6690 (4) |
| C(12) | 2039 (1) | 5096 (2) | 7584 (7) |
| H(2) | 541 (23) | 2620 (56) | 8899 (39) |
| H(3) | 920 (28) | 4096 (70) | 10619 (38) |
| H(4) | 1387 (28) | 7020 (70) | 10711 (38) |
| H(5) | 1555 (23) | 8959 (56) | 9096 (39) |
| H(7) | 1506 (18) | 9733 (40) | 6995 (29) |
| H(8) | 1554 (24) | 9007 (65) | 5226 (40) |
| H(9) | 1242 (33) | 6027 (28) | 4408 (52) |
| H(10) | 621 (24) | 3176 (65) | 5044 (40) |
| H(11) | 336 (18) | 2421 (40) | 6767 (29) |
| H(12A) | 2251 (19) | 4877 (16) | 6013 (41) |
| H(12B) | 2486 (20) | 4795 (17) | 8195 (43) |

(which numbered 719), and 230 reflexions, randomly distributed in the latter range, with $I<3 \sigma(I)$. The final set of data (which consisted of 2398 reflexions, including 120 with $I<0$ ) was used for full-matrix leastsquares refinement of the structure, assuming anisotropic temperature factors for P and F atoms, and isotropic $B$ 's for the cation atoms. The final values for this conventional refinement were $R=0.076$ and $R_{w}=$ 0.072 on the 2278 observed reflexions. The corresponding positional parameters of BDP are those utilized in performing the constrained refinement of the $\mathrm{BF}_{4}^{-}$salt (see above). From these, the electron density map reported in Fig. 5 was computed; it shows that resolution of all atoms along the annulene perimeter [with the exception of the pair constituted by $\mathrm{C}(1)$ and $\left.\mathrm{C}\left(1^{\prime}\right)\right]$ has been achieved. Distances between various atom pairs are in fact $>0.5 \AA$, to be compared with $d_{\text {min }}=0.45 \AA$ for the collected data.
At this stage, a difference map showed that the isotropic treatment of the cation was inadequate. On the other hand, anisotropic refinement of the BDP cation, although lowering the $R$ and $R_{w}$ values to 0.060 and 0.054 , respectively, was clearly misleading, since several atoms showed high interactions between their positional and thermal parameters (correlation coefficients $>0.7$ ). To avoid these interactions, TLS constrained refinement was performed, assuming (i) $4 / \mathrm{mmm}$ symmetry for the $\mathrm{PF}_{6}$ group, and (ii) $m$ symmetry for the BDP cation, whose H atoms were included in the thermal constraint. After a few cycles of refinement, convergence was assumed when no parameter shift was $>0 \cdot 5 \sigma$. The final $R$ and $R_{w}$ based on 70 independent parameters were 0.066 and 0.060 respectively.


Fig. 6. The BDP cation viewed along a principal axis of inertia. (a) Bond lengths $(\AA)$, bond angles $\left(^{\circ}\right.$ ) and torsional angles $\left(^{\circ}\right.$ ) along the annulene perimeter. (b) Dihedral angles $\left(^{\circ}\right.$ ). The values refer to the model obtained from constrained refinement (see text.)


Fig. 7. The packing of the $\mathrm{PF}_{6}^{-}$salt. Only ordered models for BDP are shown.

Table 5. Rigid-body-motion parameters for the $\mathrm{PF}_{6}$ salt

The tensors are referred to a Cartesian coordinate system coincident with the principal inertial axes $L, M$ and $N$ of the two ions. All components of the tensors have been multiplied by $10^{4}$.

|  | $\mathrm{PF}_{6}^{-}$ | BDP |
| :--- | :---: | :---: |
| $T_{11}\left(\AA^{2}\right)$ | $339(2)$ | $139(7)$ |
| $T_{22}$ | $182(2)$ | $160(5)$ |
| $T_{33}$ | $199(2)$ | $266(10)$ |
| $T_{12}$ | 0 | $13(4)$ |
| $T_{23}$ | $-30(1)$ | 0 |
| $L_{11}\left(\mathrm{rad}^{2}\right)$ | $74(2)$ | $175(4)$ |
| $L_{22}$ | $111(3)$ | $21(1)$ |
| $L_{33}$ | $169(2)$ | $36(3)$ |
| $L_{12}$ | 0 | $4(3)$ |
| $L_{23}$ | $-31(2)$ | 0 |
| $S_{11}(\AA \mathrm{rad})$ | 0 | 0 |
| $S_{12}$ | $6(1)$ | 0 |
| $S_{13}$ | $-9(1)$ | $-41(4)$ |
| $S_{21}$ | $-4(2)$ | 0 |
| $S_{22}$ | 0 | 0 |
| $S_{23}$ | 0 | $-10(3)$ |
| $S_{31}$ | $-13(2)$ | $4(2)$ |
| $S_{32}$ | 0 | $8(2)$ |
| $S_{33}$ | 0 | 0 |
| Eigenvalues of $\mathbf{L}\left(\mathrm{rad}^{2}\right)$ | 0.0186 | 0.0176 |
|  | 0.0095 | 0.0036 |
|  | 0.0074 | 0.0021 |

The final positional coordinates are reported in Table 4, and the corresponding geometry for BDP in Fig. 6. Rigid-body-motion parameters are listed in Table 5. A view of the structure, as seen down the $b$ axis, is shown in Fig. 7.

A final density map showed some relatively high residuals (maximum value $0.5 \mathrm{e} \AA^{-3}$ ) in the proximity of both ions; they may be due to errors in the data and/or in the models. In any event the geometry of the cation, as extracted from our treatment, can be considered sufficiently accurate to distinguish the preferred structure of this system, which can be safely considered an annulenium ion $[C(1) \cdots C(6)=2.293 \AA]$.

In spite of the disorder, two contacts between ions are below the sum of van der Waals radii. They are $\mathrm{C}(3)_{x y z} \cdots \mathrm{C}(10)_{-x, 1-y, \frac{1}{2}+z}=3 \cdot 355 \AA$ and $\mathrm{C}(10)_{x y z} \cdots$ $\mathrm{C}(10)_{-x, 1-y, 1-z}=3 \cdot 350 \AA$.

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[^0]:    * In the program used for constrained refinement, the TLS tensors are referred to the system defined by the inertial axes. All components of the tensor $\mathbf{S}$ are zero owing to symmetry requirements of the space group.
    $\dagger$ Lists of structure factors and anisotropic thermal parameters for the tetrafluoroborate and hexafluorophosphate salt structures have been deposited with the British Library Lending Division as Supplementary Publication No. SUP 34369 (19 pp.). Copies may be obtained through The Executive Secretary, International Union of Crystallography, 5 Abbey Square, Chester CHI 2HU, England.

